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Preface

Stein's method has seemed wildly different, are tantalizing connections remain vague. Most on complex dependent quality error bounds.

For all these virtues of Stein's method. The applications and examples Markov chains, approximations for statistical mechanics.

These papers were prepared at Stanford's method at Stanford's NSF grant we were able Reinert) and on Mark Yan). Central to the Stanford has a lively, fun students so our weekl accessible. Margaret highlight by organizing Rick Vitale, to whom

A theme of the work method to derive approximations and μ_0 an approximation of an exchangeable process approximation by μ_0

Usually the proofs provide an exchangeable pair (W, W') given transitions $K(w, w')$ and This gives rise to a variety of approximations.

These ideas are published by Gesine Reinert. The paper is a hybrid approach.

It is hard to convey the full picture, but when he talks about lemmas, propositions, years he has taken up with numerics. Some of his work has had a significant impact on the method. We look forward to